## Waiting Strategies for the Dynamic and Stochastic Traveling Salesman Problem

## Gianpaolo Ghiani<sup>1,\*</sup>, Gilbert Laporte<sup>2</sup>, Emanuele Manni<sup>1</sup>, and Roberto Musmanno<sup>3</sup>

<sup>1</sup>Dipartimento di Ingegneria dell'Innovazione University of Salento via per Monteroni 73100, Lecce, Italy

<sup>2</sup>Canada Research Chair in Distribution Management HEC Montréal 3000, chemin de la Côte-Sainte-Catherine

## Montréal, Canada H3T 2A7

<sup>3</sup> Dipartimento di Elettronica, Informatica e Sistemistica University of Calabria via P. Bucci 41C 87036 Rende (CS), Italy

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**Abstract**—In the *Dynamic and Stochastic Traveling Salesman Problem* (DSTSP) a vehicle has to service a number of requests which are disclosed in a dynamic fashion over a planning horizon. When the vehicle is temporarily idle, one option is to reposition it in anticipation of future demand. The aim of this paper is to study waiting strategies for the DSTSP under a probabilistic characterization of customer requests. We determine an optimal policy through a Markov decision process and we develop both lower and upper bounds (analytically and heuristically, respectively) on the optimal policy cost. The behavior of these procedures is illustrated on a numerical example and tested on a set of random instances.

Keywords-Traveling Salesman, Real-time fleet management, Markov decision processes, Transportation.

<sup>\*</sup> Corresponding author's email: emanuele.manni@unile.it